

Evaluation of Heuristic Algorithms for Optimizing Resource Assignments in LTE-A

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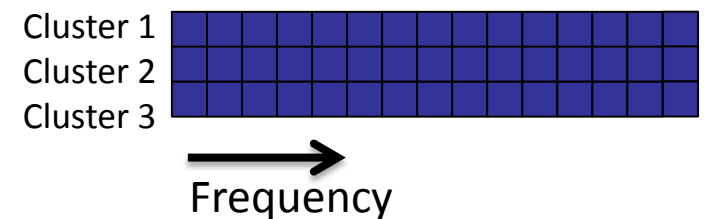
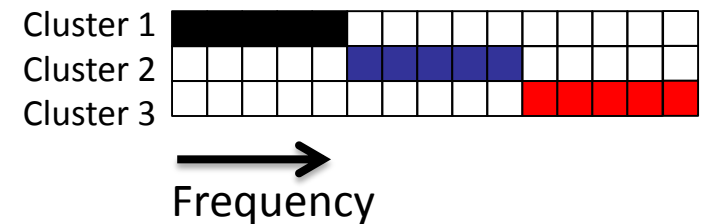
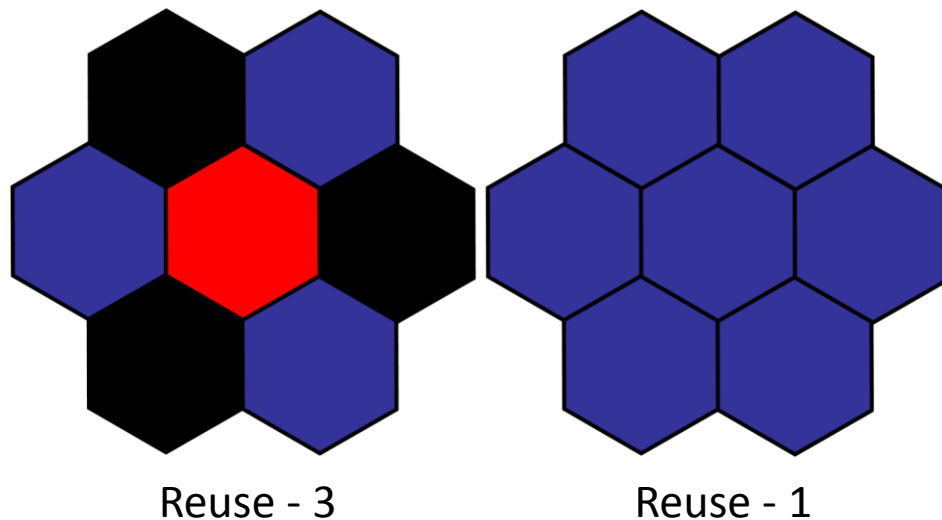
Problem Formulation

Heuristic Algorithms

Simulation Results

LTE Resource Management

- ▶ LTE has a frequency reuse factor of one
- ▶ Interference mitigation is important
- ▶ Cooperatively managing resource assignments of multiple cells
- ▶ Increasing the aggregated system throughput
- ▶ Therefore increasing Cell Spectral Efficiency (CSE)



Scheduling decisions

- ▶ Resources in frequency and time
- ▶ Modulation and coding scheme
- ▶ Transmission power
- ▶ Precoding (MIMO)

Objectives

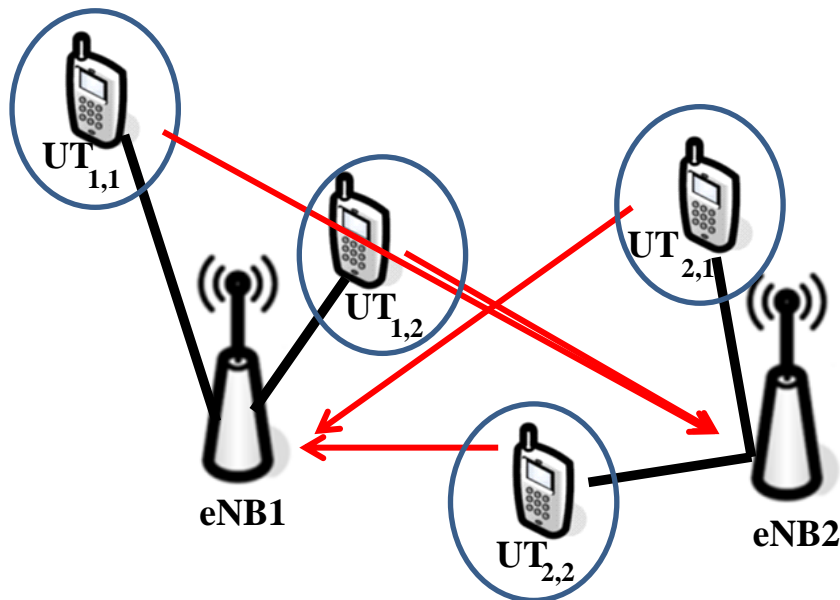
- ▶ Individual best throughput
- ▶ Best system throughput → Coordination
- ▶ Increasing cell edge user throughput → Coordination

Nonlinear optimization problem

- ▶ Mapping of SINR to data rates using nonlinear functions
- ▶ SINR depending on several interfering users
- ▶ Needs simplification!

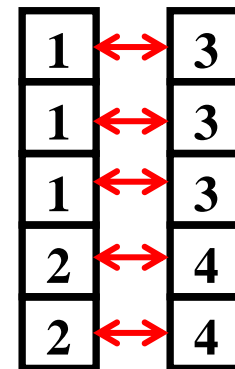
Simplification

- ▶ Each user has equal amount of resources
- ▶ Same amount of UTs per eNB (in one TTI)
- ▶ Each UT has only one interfering UT per other base station
- ▶ Calculate data rates depending on SINR before optimization



Example of possible resource assignment

eNB1 eNB2



Phys. Resource Block



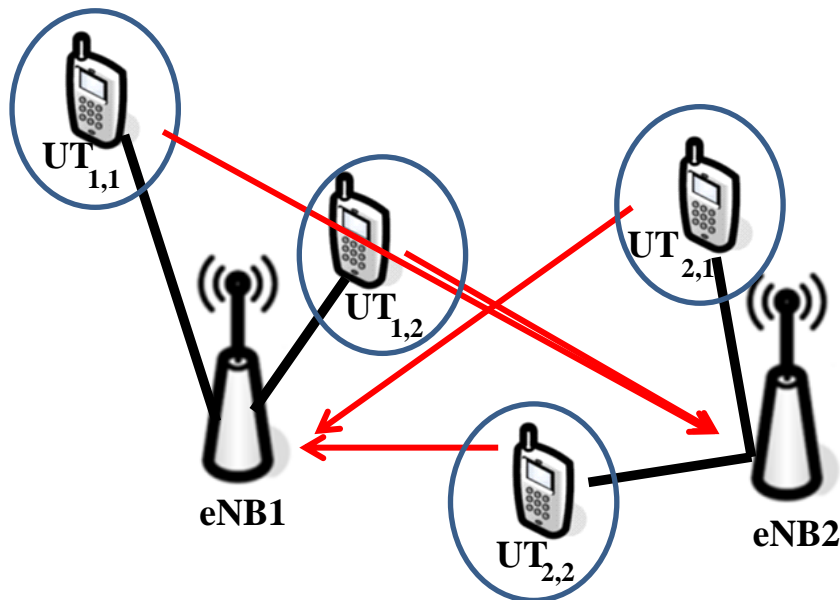
PRB assigned to UT u

— Signal

— Interfering signal

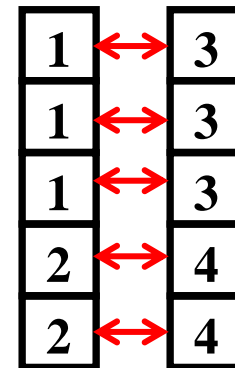
Optimizing resource assignment of user terminals

- ▶ Which UTs transmit on same resources?
- ▶ Linear Assignment Problem



Example of possible resource assignment

eNB1 eNB2



Phys. Resource Block



PRB assigned to UT u

— Signal

— Interfering signal

Linear Assignment Problem

Which user terminals transmit on the same resources

- ▶ Assigning user terminals
- ▶ Optimal solvable in polynomial time
- ▶ Hungarian/Munkres Algorithm

UT _{2,1}	$r_{1,1}$	$r_{2,1}$		$r_{ S_2 ,1}$
UT _{2,2}	$r_{1,2}$	$r_{2,2}$		$r_{ S_2 ,2}$
⋮			⋱	
UT _{2, S_1}	$r_{1, S_1 }$	$r_{2, S_1 }$		$r_{ S_2 , S_1 }$
UT _{1,1}	UT _{1,2}	⋯	UT _{1, S_2}	

$$\max \sum_{i=1}^N \sum_{j=1}^N c_{i,j} r_{i,j}$$

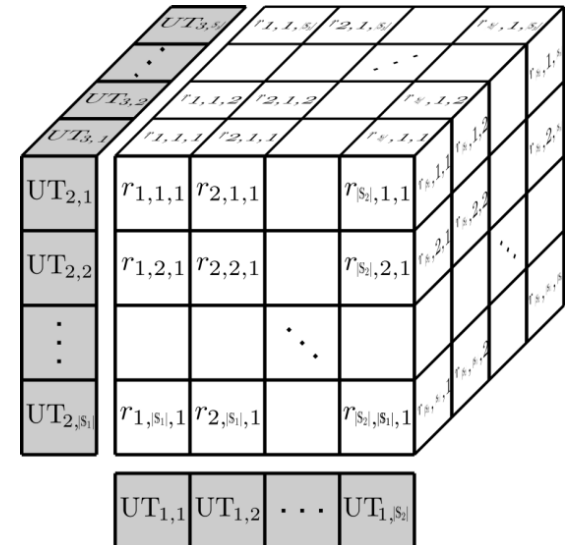
$r_{i,j}$: Elements of matrix
with throughputs (rates)

$c_{i,j}$: Elements of permutation
matrix ($c_{i,j} \in \{0, 1\}$)

Multidimensional Assignment Problem

For more than two base stations

- ▶ Multidimensional Assignment Problem
- ▶ Number of assignments: $(\#UT!)^{\#BS} - 1$
- ▶ NP-hard problem
- ▶ Heuristic algorithms



1. Greedy Heuristic
2. Max Regret Heuristic
3. Greedy randomized adaptive search procedure (GRASP)

Simply always takes the assignment with best throughput

	$UT_{1,1}$	$UT_{1,2}$	$UT_{1,3}$	$UT_{1,4}$
$UT_{2,1}$	7	36	44	19
$UT_{2,2}$	20	30	40	28
$UT_{2,3}$	12	22	21	9
$UT_{2,4}$	14	4	19	13

$$L = \{44, 30\}$$

Solution found by Greedy heuristic: 97

Optimal solution: 108

Maximum Regret Heuristic

Calculates “regret” and takes the respective assignment

	UT _{1,1}	UT _{1,2}	UT _{1,3}	UT _{1,4}	
UT _{2,1}	7	36	44	19	17
UT _{2,2}	20	30	40	28	-
UT _{2,3}	12	22	21	9	5
UT _{2,4}	14	4	19	13	1
	2	14	-	3	

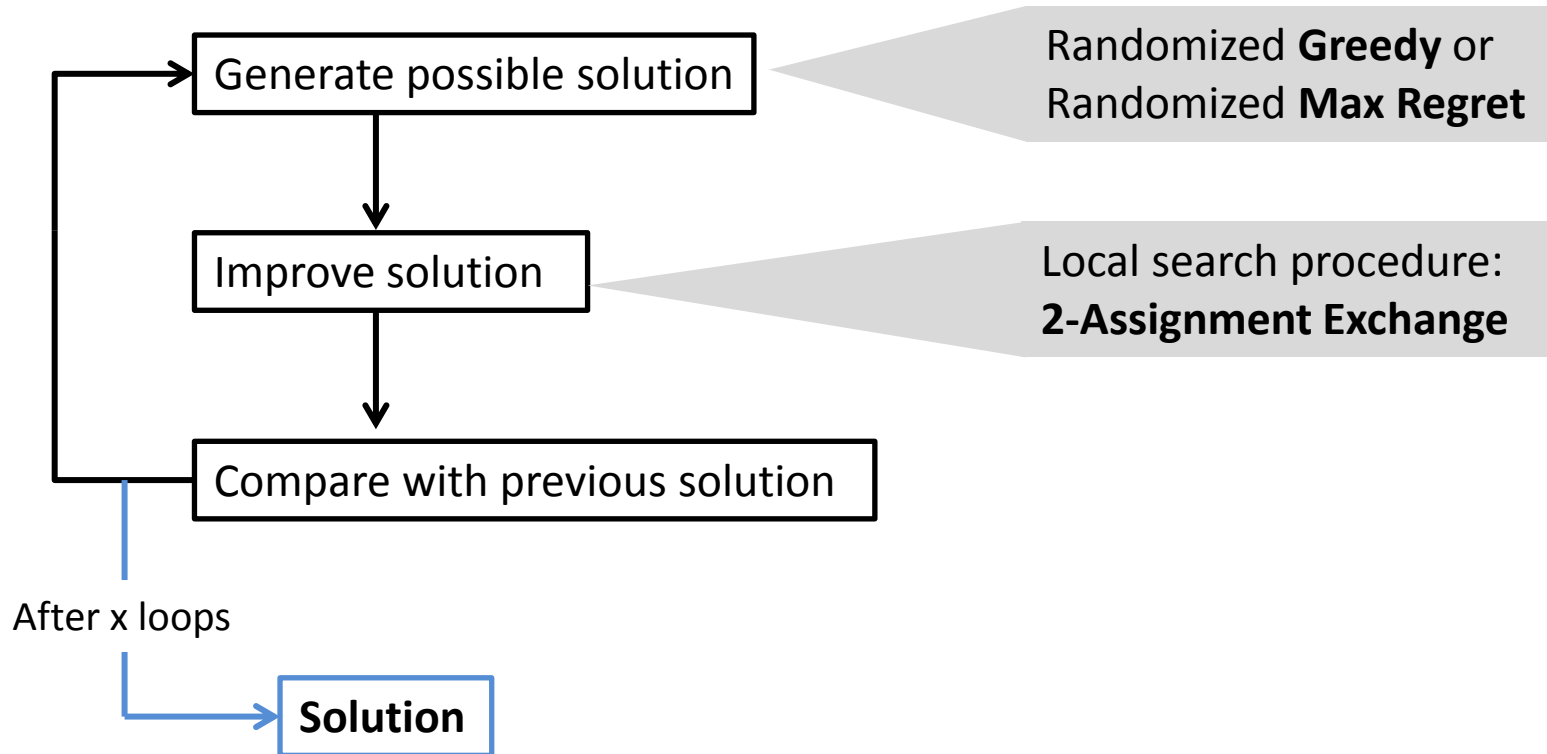
$L = \{40, 36\}$

Solution found by Greedy heuristic: **97**

Solution found by Maximum regret heuristic: **101**

Optimal solution: **108**

Greedy Randomized Adaptive Local Search Procedure (GRASP)



Randomized Greedy

- ▶ Taking more than the highest value into account
- ▶ Picking one at random
- ▶ Randomized Max Regret similar

	UT _{1,1}	UT _{1,2}	UT _{1,3}	UT _{1,4}
UT _{2,1}	7	36	44	19
UT _{2,2}	20	30	40	28
UT _{2,3}	12	22	21	9
UT _{2,4}	14	4	19	13

$L = \{36\}$

	UT _{1,1}	UT _{1,2}	UT _{1,3}	UT _{1,4}
UT _{2,1}	7	36	44	19
UT _{2,2}	20	30	40	28
UT _{2,3}	12	22	21	9
UT _{2,4}	14	4	19	13

$L = \{36\}$

	UT _{1,1}	UT _{1,2}	UT _{1,3}	UT _{1,4}
UT _{2,1}	7	36	44	19
UT _{2,2}	20	30	40	28
UT _{2,3}	12	22	21	9
UT _{2,4}	14	4	19	13

$L = \{36, 40\}$

Example of randomized Greedy for a two-dimensional assignment problem

Two Assignment Exchange

- ▶ Takes calculated solution
- ▶ Exchange of adjacent assignments
- ▶ Takes the better assignment

	UT _{1,1}	UT _{1,2}	UT _{1,3}	UT _{1,4}
UT _{2,1}	7	36	44	19
UT _{2,2}	20	30	40	28
UT _{2,3}	12	22	21	9
UT _{2,4}	14	4	19	13

$$L = \{44, 30, 14, 9\}$$

	UT _{1,1}	UT _{1,2}	UT _{1,3}	UT _{1,4}
UT _{2,1}	7	36	44	19
UT _{2,2}	20	30	40	28
UT _{2,3}	12	22	21	9
UT _{2,4}	14	4	19	13

$$44 + 30 < 40 + 36$$

	UT _{1,1}	UT _{1,2}	UT _{1,3}	UT _{1,4}
UT _{2,1}	7	36	44	19
UT _{2,2}	20	30	40	28
UT _{2,3}	12	22	21	9
UT _{2,4}	14	4	19	13

$$L = \{40, 36, 14, 9\}$$

Example of two assignment exchange for two-dimensional assignment problem

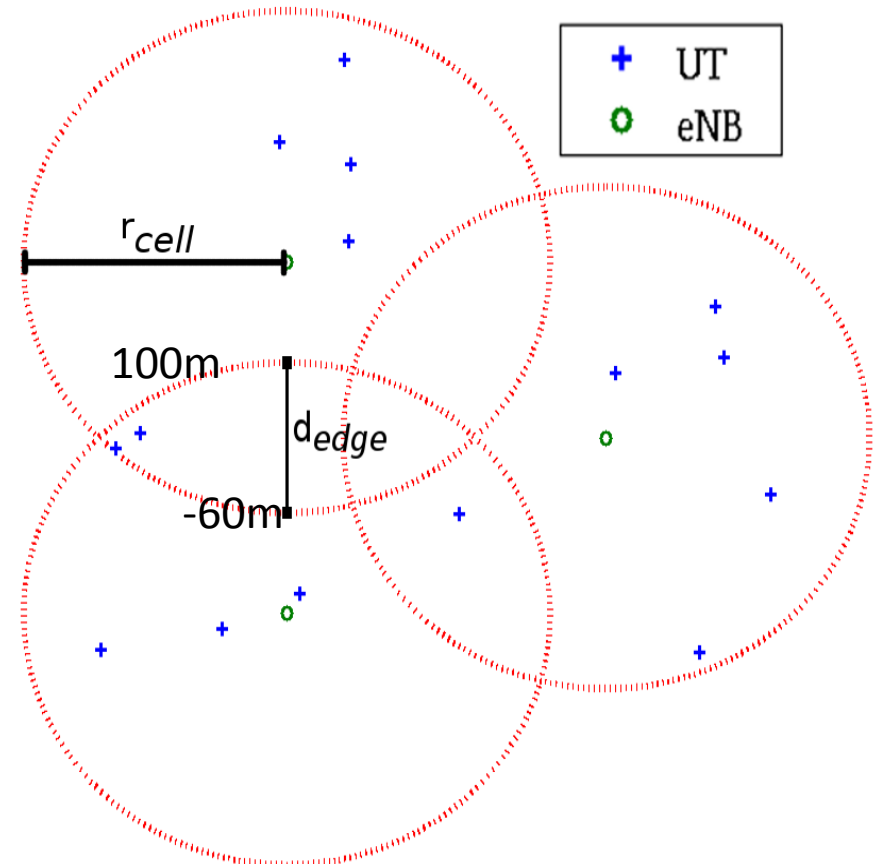
Simple LTE model in MATLAB

- ▶ 5 UTs per eNB
- ▶ 2 to 4 eNBs
- ▶ $d_{\text{edge}} = -200\text{m}$ to 100m
- ▶ $r_{\text{cell}} = 100\text{m}$
- ▶ Path-loss model: InH NLoS
- ▶ Bandwidth: 20MHz

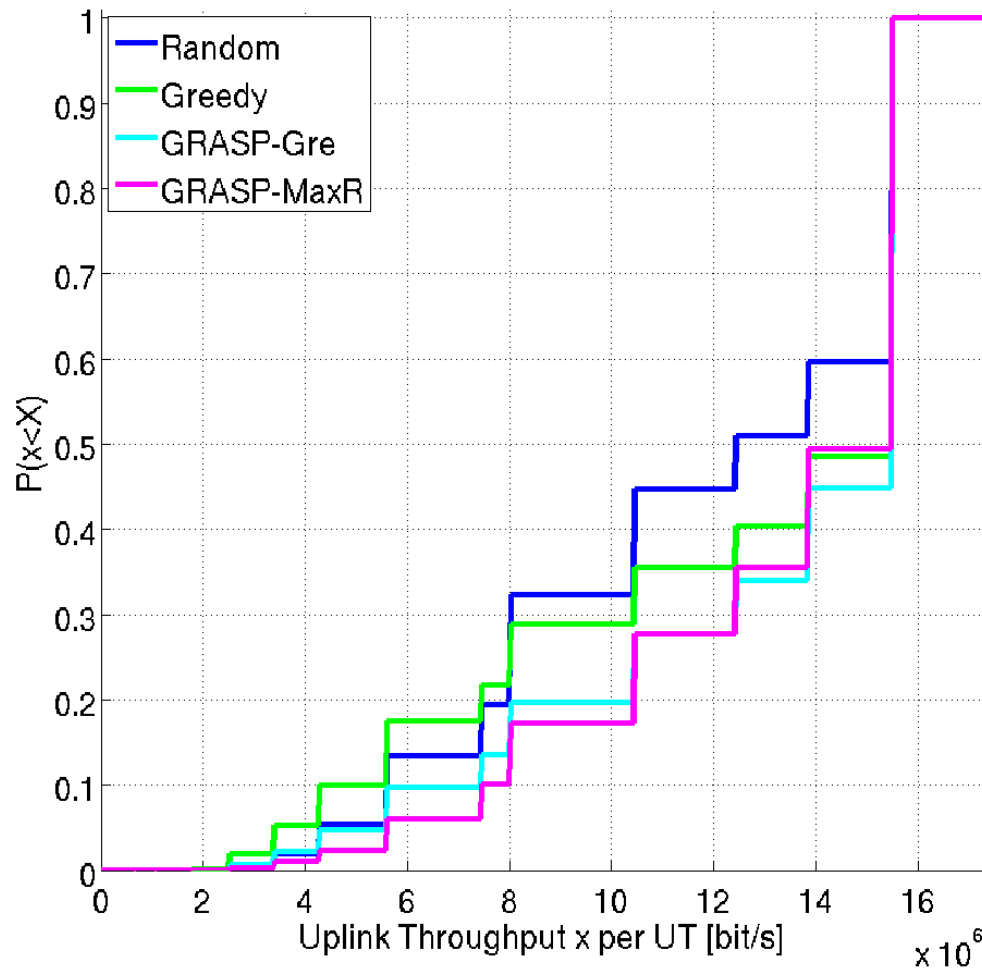
Algorithm parameter

- ▶ 4 loops of GRASP
- ▶ 3 highest values in randomized Greedy / Max Regret

Algorithm results compared to random assignment



CDF of Uplink Throughput ($d_{edge} = 0$ m)



$r_{cell}: 100$ m

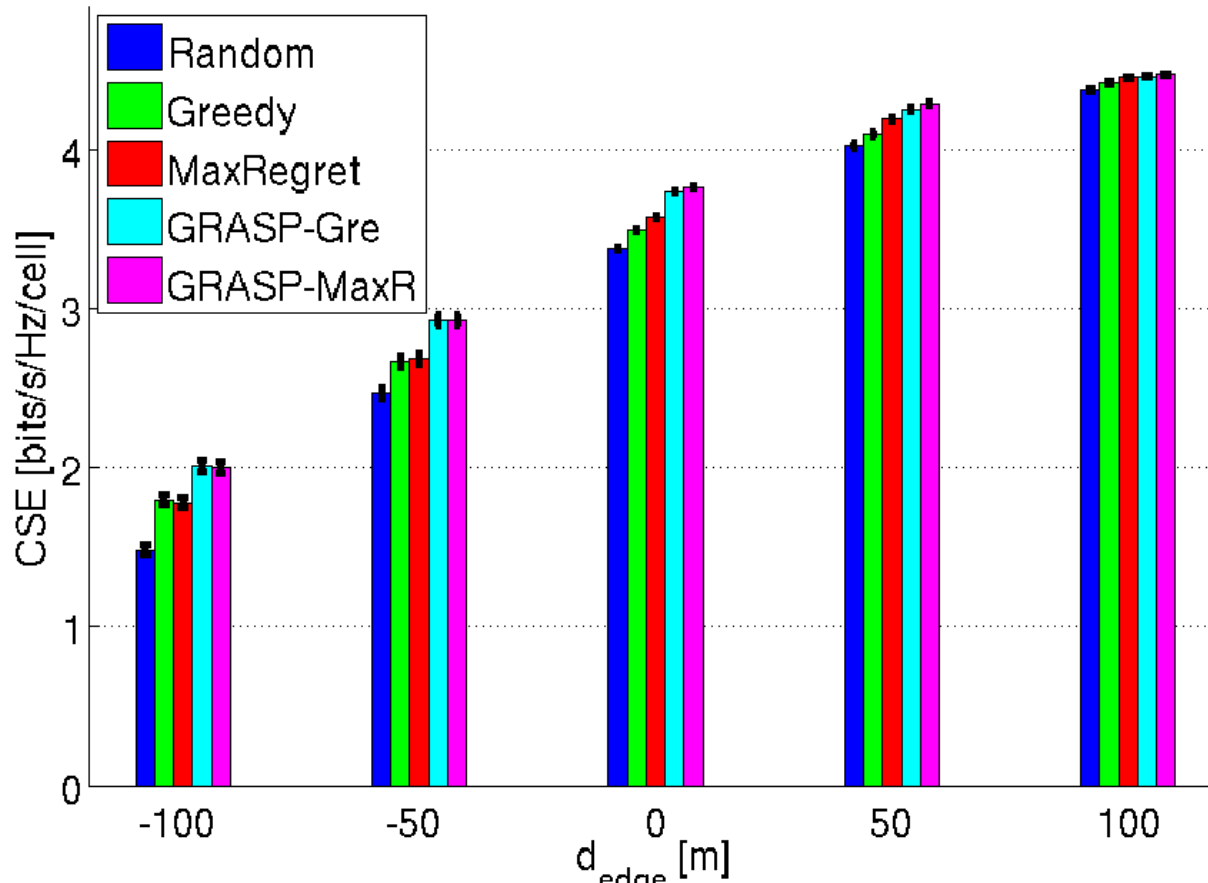
$d_{edge}: 0$ m

3 Cells

5 User Terminals

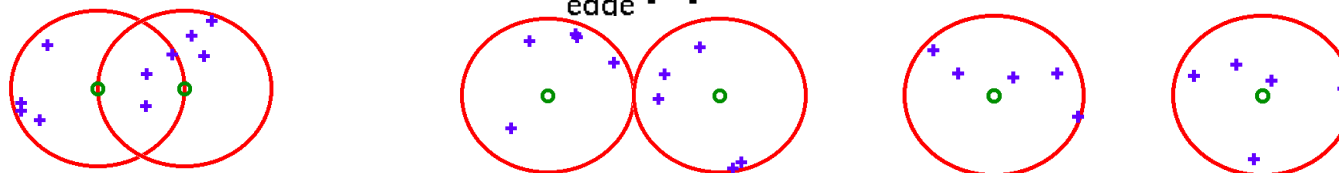
Cell Spectral Efficiency

Cell Spectral Efficiency over d_{edge}



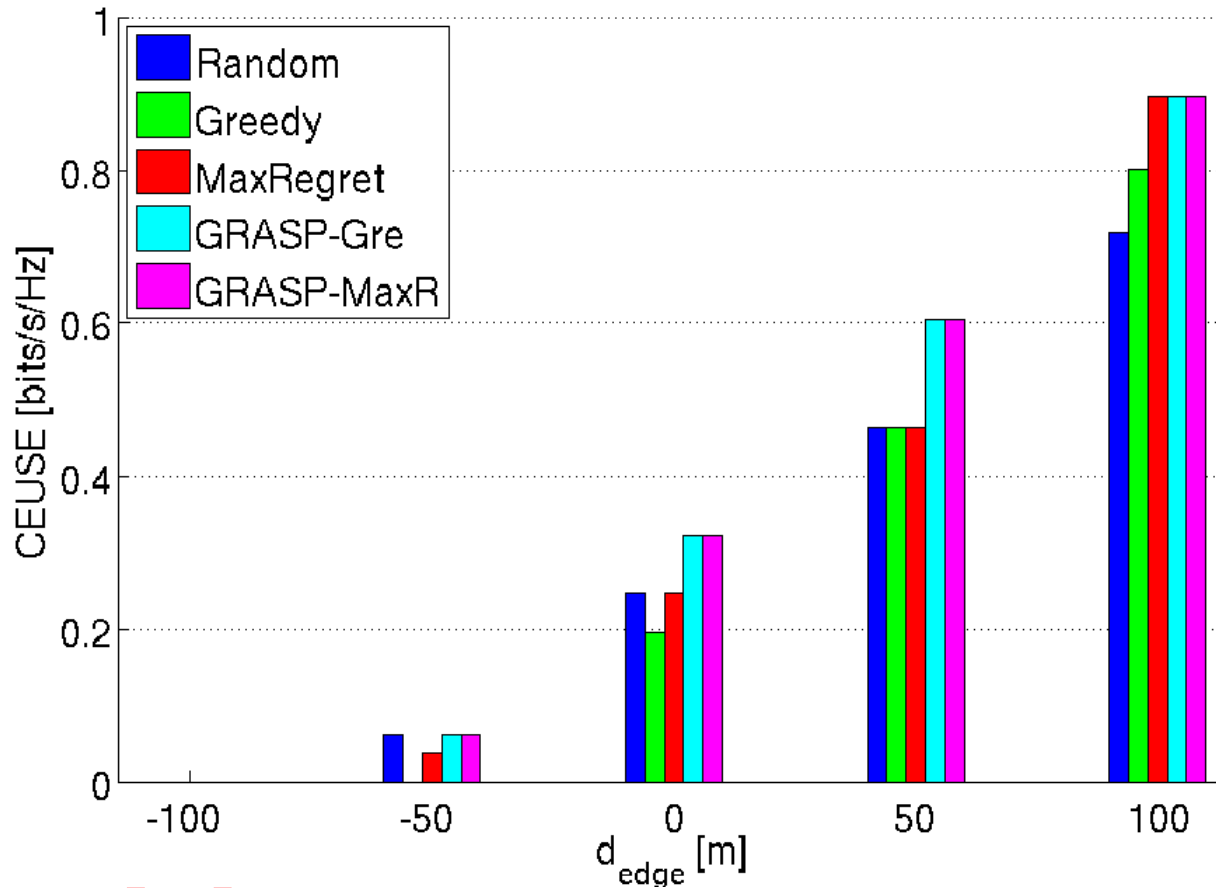
r_{cell} : 100m
 d_{edge} : -100m to 100m

3 Cells
5 User Terminals



Cell Edge Users

Cell Edge User Spectral Efficiency over d_{edge}

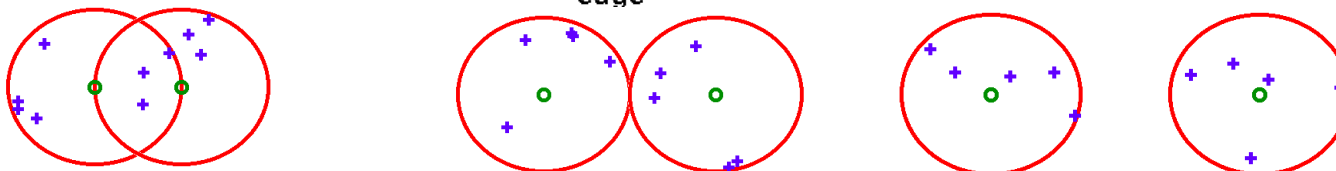


r_{cell} : 100m

d_{edge} : -100m to 100m

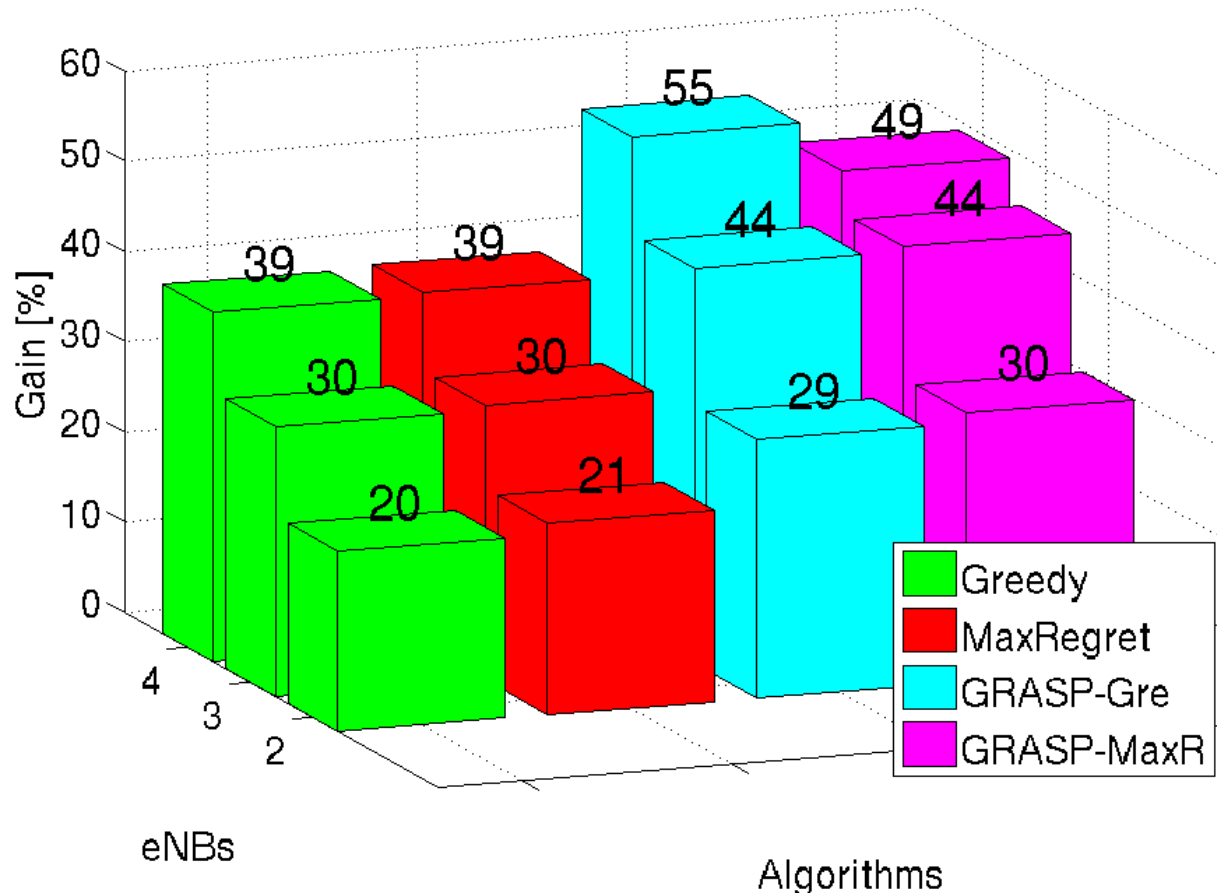
3 Cells

5 User Terminals



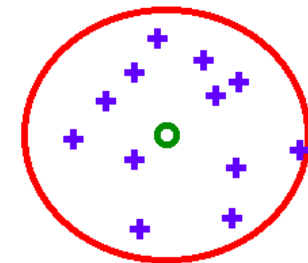
Gain in CSE over Random Assignment

CSE Gain compared to Random



r_{cell} : 100m
 d_{edge} : -200m

2 to 4 Cells
5 User Terminals



Summary

- ▶ Resource assignment problem formulated as Multidimensional Assignment Problem

Conclusion

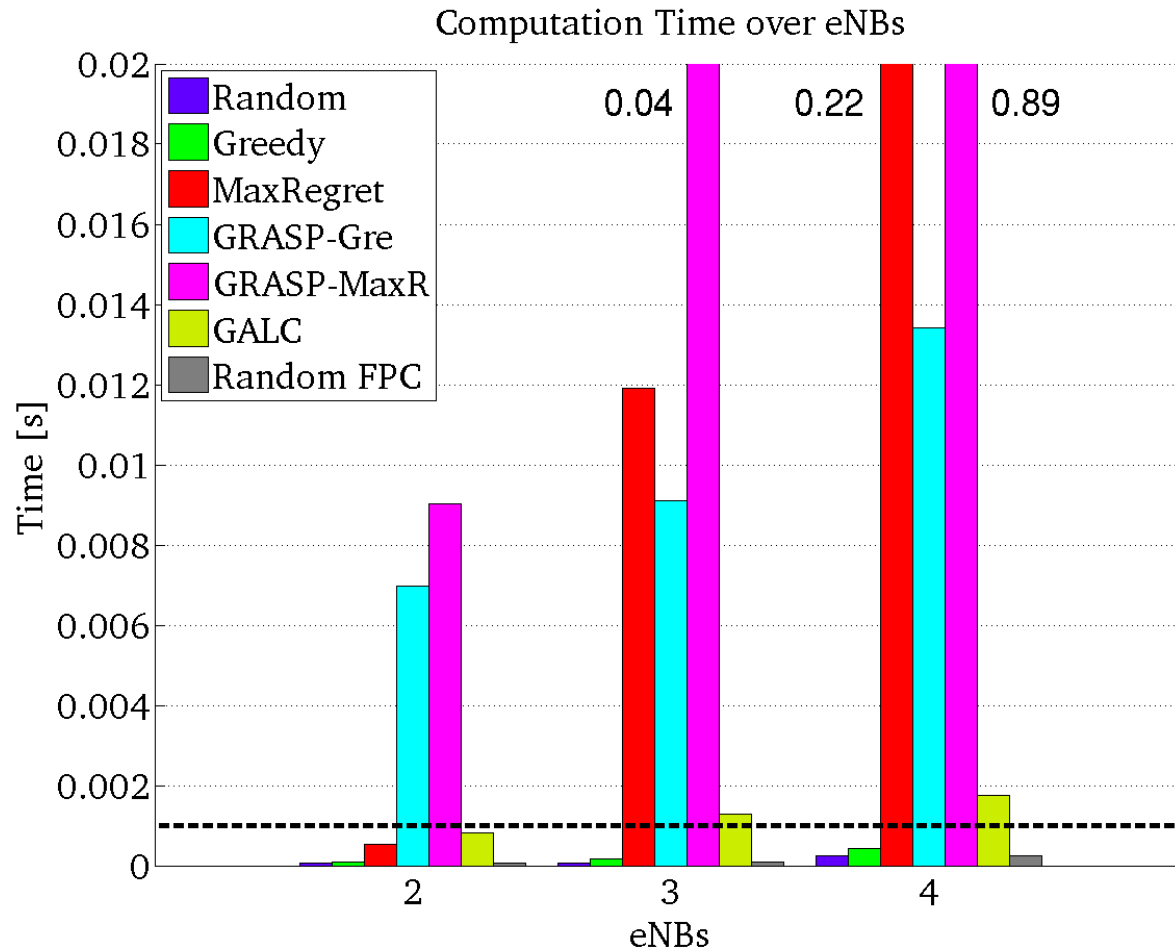
- ▶ Metaheuristic GRASP shows better performance for Cell Spectral Efficiency (CSE) and Cell Edge User Spectral Efficiency (CEUSE) than other heuristics
- ▶ In some scenarios improvement of more than 50% compared to random assignment

Outlook

- ▶ Evaluation in system level simulator
- ▶ Relax restriction of same amount of Resource Blocks per UT and UTs per cell

Thank you for your attention.

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Computation time with 6 UTs per eNB